# Power Cycles and Energy Storage John C. Bean 

Outline

How to meet our daily cycle of electrical power consumption
Today's scenario: Base Load Power Plants (24/7) + Dispatchable Power Plants (evening only)
Possible future scenario: Base Load Plants + Massive Energy Storage
Candidates for Massive Energy:
Pumped Storage Hydro
Hydrogen Fuel Cells
Flywheel Energy Storage
Compressed Air Energy Storage (CAES)
Capacitor / Super Capacitor Energy Storage
Battery Energy Storage
Molten Salt Heat Energy Storage
How much of each is required for Base Load + Massive Energy Storage scenario?
More ambitious scenario of ALSO eliminating ALL non-green power sources

## Power Cycles and Energy Storage

I talk about the puzzle of designing future power systems
"Puzzle," because so many factors must be balanced to:
Provide enough affordable power
While sustaining a high quality biosphere
We've also seen that renewables are not silver bullets
If only because they demand huge natural resource commitments
Meaning that future power systems will have to combine different technologies
Today you will see how the natural cycles of power consumption and production
ALSO drive the use of different technologies
And how energy storage will become critical

## It all starts with this:

The cycles in our consumption of electrical power (and its real time cost):

www.eia.gov/todayinenergy/detail.cfm?id=12711 YELLOW midnight lines added
Note the almost sinusoidal cycles:
Peaking at 6pm (cook dinner, cool down/heat up house, do laundry . . . )
With amplitude of the oscillation equaling $\sim 40 \%$ of peak value

Simplifying a little bit, over one day:


We have a constant component at about 60\% of the peak

Plus an oscillating component moving from there up to $100 \%$ at about 6 pm
With oscillating component's average at $80 \%$ (from its symmetry)
Meaning that time averaged total power is also about $80 \%$ of the peak power

## Or dividing these two up:

The constant "base" electrical load:


Plus a variable "dispatchable" component (so called because a dispatcher controls it?)


So we could also call Scenario \#1: "Base + Dispatchable"

## Scenario \#1) Base Power Plants + Dispatchable Power Plants + no storage:

## This is TODAY's scenario, now in almost universal use

But, of course, power companies want to minimize costs (theirs and yours)
Costs come in two principal flavors: FIXED COSTS and VARIABLE COSTS
A fixed cost is just that, something you're going to have to pay no matter what
For power plants, the biggest are most often construction (capital) costs
Which are then translated into ongoing mortgage / bond payments
Which have to be paid, whatever power you are now producing
A variable cost is instead a cost that varies with the plant's power output
Which includes the labor cost of the operators as well as fuel costs

## The contrast between Base and Dispatchable Plants:

FIXED COSTS: For both base and dispachable plants are ~ mortgage payments Which depend upon building cost, mortgage interest and duration

## VARIABLE COSTS:

Base Plant = Labor \& Fuel costs while power is being produced (= all the time)
Dispatchable Plant =
Labor \& Fuel costs while power is being produced +
Labor \& Fuel costs while plant is warming up (NOT producing power) +
Labor costs while plant is shutting down (NOT producing power) +
Some labor costs 24/7, for security, maintenance, deliveries . . .
But for all but open-cycle-gas-turbine dispatchable plants (which don't use steam): Warm up time + Shut down time can easily exceed power production time!

The LCOE is still going to be hugely inflated, because it still equals:
LCOE = Levelized Cost / Energy Produced

With numerator still depending on FULL purchase/construction cost (via mortgage)
But denominator now hugely reduced: E.G., for plant operating 3 hours per day:
Denominator reduced by $(3 / 24)=1 / 8=>$ LCOE increases by $8 X$


Which is indeed seen in the blue cost of power time variation above! Which is WHY our gas "peaking" power is ~ 4 X cost of base power

## Scenario \#2) Add storage in place of dispatchable plants

Why pay for dispatchable power plants that sit idle almost all of the day!
INSTEAD: Choose the CHEAPEST CLEANEST TYPE(S) OF POWER PLANTS
Let them run ALL DAY AT FULL POWER (maximizing their bang / capital buck)
Size them so their power $=80 \%$ of peak power $=$ average daily power
And STORE EXCESS POWER produced early in the day for use later in the day

Old Scenario \#1:


New Scenario \#2:


But how MUCH energy do we have to store early in the day?

From earlier discussion, average power per day $=80 \%$ of peak power
So daily energy $=E_{\text {daily }}=0.8 P_{\text {peak }} \times 1$ day
Assuming shape of energy stored \& moved curve below is indeed sinusoidal:
From the diagram, amplitude of the sine $=(0.2 \times$ peak power $)$
Then, stored early day energy = integral (from 0 to day/2) of $0.2 \mathrm{P}_{\text {peak }} \operatorname{Sin}$

$$
=0.2 \mathrm{P}_{\text {peak }} \times \text { day } / \mathrm{Pi}=0.064 \mathrm{P}_{\text {peak }} \times \text { day }=(0.064)\left(\mathrm{E}_{\text {daill }} / 0.8\right)=8 \% \text { of } \mathrm{E}_{\text {daily }}
$$



So we could also call Scenario \#2:
"Conventional Power $+$ 8\% Storage"
U.S. energy per day value:

From the Power Plant Land and Water Requirements lecture:
Total US energy production (2012) $=4,047,765$ GW-h (1) per year
Which translates into US energy production $=11,089$ GW-h per day
So we'd need to store $8 \%$ of that early in the morning (for use later in that day):
Scenario \#2 US energy storage required per day = 887 GW-h


So with that target figure in mind, what are the alternatives?

## Candidate energy storage technologies:

From the U.S. Department of Energy (DOE) 2013:

Current U.S. energy storage capacity:
(ALMOST ALL of it is pumped hydro!)


## Maturity of storage technologies:

NOTE WILD EXAGGERATION!
Net U.S. Hydro storage is still tiny
And it dwarfs other 3 "Deployed"
(which at BEST = 1-2 test plants)


Nevertheless, sorting the more plausible/mature candidates:
Which fall into two categories based on naturally different figures of merit Energy storage SYSTEMS = Multi-component plants, spread over hectares:
a) Pumped Hydro Energy Storage
b) Hydrogen Fuel Cell Energy Storage
c) Flywheel Energy Storage
d) Compressed Air Energy Storage (CAES)

Energy storage THINGS = Components that would just be massively warehoused:
e) Capacitor / Super Capacitor Energy Storage
f) Battery Energy Storage
g) Molten Salt Heat Energy Storage

For each of these candidates, we need to know:

## How much is required for our \#2 energy storage scenario?

That is, storing $8 \%$ of early day energy for later use $=>887 \mathrm{GW}-\mathrm{h}$

For all candidates, this involves their "round trip return efficiency"
Because energy returned = energy put in x return efficiency
For energy storage SYSTEMS, we need their plant footprint \& storage capacity
In order to work out total number of plants and size required
For energy storage THINGS we need their energy storage density (kW-h / m³)
We could then assume, say, that they'd be warehoused ~1 meter high
Combining => Net national size of such energy storage warehouses
And for all candidates, we need their projected levelized cost

## a) Energy storage via Pumped Storage Hydro (PSH)

The best current way to store power
Which, in my Hydropower / Windpower lecture I represented thusly:


But data from previous lecture was incomplete, so we must slow down:

An Introduction to Sustainable Energy Systems: WeCanFigureThisOut.org/ENERGY/Energy_home.htm

## The Bath County Virginia pumped hydro storage plant:

## From Dominion Power's website: ${ }^{1}$

"The World's Biggest Battery" - but no numbers!
Supplies "over $1 / 2$ million customers with (peak) power"
At rate "exceeding Hoover Dam"

13.5 million gallons / minute ( $852 \mathrm{~m}^{3}$ / sec)

Area of upper reservoir $=265$ acres $\left(1.07 \times 10^{6} \mathrm{~m}^{2}\right)$
Its "water level fluctuates 105 feet ( 32 meters) during operation"
OK, now we have finally got enough information to calculate energy stored!

1) Link to webpage: www.dom.com/about/stations/hydro/bath-county-pumped-storage-station.jsp

Energy stored in Bath pumped storage energy plant:

Water's energy as it falls down into lower reservoir:
$\Delta \mathrm{E}=\mathrm{Mgh}=\rho_{\text {water }} \times$ (volume of water moved) $\times \mathrm{g} \times$ (height difference)
$\rho_{\text {water }}=1000 \mathrm{~kg} / \mathrm{m}^{3} \quad \mathrm{~g}=9.8 \mathrm{~m} / \mathrm{sec}^{2}$
height difference $=385$ meters
volume of water moved $=\left(1.07 \times 10^{6} \mathrm{~m}^{2}\right)(32$ meters $)$
$\Delta E=\left(1000 \mathrm{~kg} / \mathrm{m}^{3}\right)\left(1.07 \times 10^{6} \mathrm{~m}^{2}\right)(32$ meters $)\left(9.8 \mathrm{~m} / \mathrm{sec}^{2}\right)(385 \mathrm{~m})$
$=1.29 \times 10^{14} \mathrm{~kg} \mathrm{~m} / \mathrm{s}^{2}=1.29 \times 10^{14}$ Joules
$=1.29 \times 10^{14} /(3,600,000,000) \quad \mathrm{MW}-\mathrm{h}=35.8 \mathrm{MW}-\mathrm{h}$
Bath upper reservoir $=265$ acres $=1.07 \mathrm{~km}^{2}$
If lower reservoir were reduced to same size $=>\mathbf{~} \mathbf{2} \mathbf{k m}^{2}$ reservoir area

## Round trip energy efficiency of pumped storage hydro?

Its largely limited by the HUGE electrical motor/generators/turbines required
Motors drive the turbines driving the water UP the hill, then:
Water turns turbines driving generators as it falls back DOWN

But some power may also be lost by turbulence-induced heating of the water itself

Overall power recovery, after accounting for all possible losses?
Various sources give efficiencies from $70 \%{ }^{1}$ to $85 \%{ }^{2}$
I'll go with the NREL study ${ }^{3}$ number: $80 \%$ efficiency
b) Fuel cell based energy storage:

Idea as depicted in an NREL presentation: ${ }^{1}$

U.S. National Renewable Energy Lab: "Analysis of Hydrogen and Competing Technologies for Utility-Scale Energy Storage"

Fuel cell based storage has three stages:

- Electrochemical cell \# 1 uses electrical energy to electrolyze water:
$\mathrm{H}_{2} \mathrm{O}+$ electrical energy $=>\mathrm{H}_{2}+1 / 2 \mathrm{O}_{2}$
- Gaseous $\mathrm{H}_{2}$ (and possibly $\mathrm{O}_{2}$ ) are then stored in pressurized tanks
- When energy is needed, gases are sent into Electrochemical cell \#2:
$\mathrm{H}_{2}+1 / 2 \mathrm{O}_{2}=>\mathrm{H}_{2} \mathrm{O}+$ electrical energy
ONE electrochemical cell COULD do both things ( $\sim$ charging/discharging of battery) But, apparently to optimize designs, input \& output cells are separate

ALTERNATIVE: Stored $\mathrm{H}_{2}$ is instead sent to a gas turbine generator
Eliminating fuel cell \#2
Likely less efficient but also likely reducing capital cost

## Fuel cell energy storage numbers?

From earlier Batteries and Fuel cell lecture:


Poor round trip efficiencies:
Only 30-35\% !
U.S. National Renewable Energy Lab:
"Hydrogen for Energy Storage Analysis
Overview"
http://www.nrel.gov/hydrogen/pdfs/48360.pdf

What about energy storage density? It's very complicated:
"Storage" is in tanks, but RATE of energy storage and release
Will depend on size of input and output electrochemical cells
NREL's design studies are for 300 MW-h storage plants
But are now storing energy from single 10 kW wind turbine (i.e. ~ $50 \mathrm{~kW}-\mathrm{h}$ )
c) Flywheel based energy storage:

Maximum possible energy stored:

$$
\begin{aligned}
E_{\max } & =K \times M \times \sigma / \rho \\
K & =\text { "flywheel shape factor" } \\
M & =\text { flywheel mass } \\
\sigma & =\text { tensile strength of material } \\
\rho & =\text { density of material }
\end{aligned}
$$


https://en.wikipedia.org/wiki/Flywheel_energy_storage

Why doesn't formula contain rotation speed? And why include tensile strength?
Because strategy is to run flywheel so fast it almost tears itself apart!
Thus almost-destructive-speed is what formula seemingly assumes
Round trip energy recovery efficiency? Energy is lost to heat in rotation bearings Conventional bearings: "20-50\% energy loss in two hours"

Magnetic levitation bearings: 85\% round trip energy efficiency

## Flywheel energy storage numbers?

Web search produced information on only two experimental grid storage projects:
Beacon Power in Hazle Township, Pennsylvania - completion 2015 (?) ${ }^{1}$
Rhode, County Offalay, Ireland - completion 2017 2-4
Data: Storage targets: Beacon 25 kW-h / Rhode 2 MW-h
Pennsylvania: 200 flywheels (as depicted at right)
Ireland: Projected efficiency: 85-90\%


Carbon fibers / magnetic bearings / vacuum
Size? / Power storage density? Found no direct data
But from this picture is of Irish site ${ }^{3}$
Footprint: ~ 2 hectares $=0.02$ km²


1) http://energy.gov/sites/prod/files/2015/05/f22/Beacon-Power-Flywheel-Aug2013.pdf
2) http://www.theguardian.com/environment/2015/apr/08/new-energy-storage-plant-could-revolutionise-renewable-sector
3) http://www.rte.ie/news/business/2015/0326/689945-renewable-energy-storage/
http://schwungrad-energie.com/projects/rhode-hybrid-test-facility/

## d) Compressed air energy storage (CAES):

## Idea is potentially large scale:

Compress air into tank or reservoir / Release air to drive turbine generator


It sounds like you just need to invoke the Ideal Gas Law:
$\mathbf{P V}=\mathbf{n} \mathbf{R} \quad$ where $\mathrm{R}=$ the ideal gas constant
But rework this and you can spot a problem: $\mathbf{P}=\mathbf{n} \mathbf{R}(\mathbf{T} / \mathbf{V})$
So if you increase the pressure of a gas (P), what happens?
Does temperature ( T ) increase? Does volume $(\mathrm{V}$ ) decrease? OR both?
REALITY CHECK: Try touching an air compressor, or even a bicycle tire pump
Actually don't, you'll burn your hand because compressing gas => heat
Refrigerators, air conditioners, and heat pumps are ALL partially based on:

- Fact that pressurizing gases HEATS them
- Fact that depressurizing gases COOLS them


## Faced by this reality, Wikipedia et al. ignore it

They pretend temperature stays constant, allowing them to use only Ideal Gas Law
But this also makes calculation of CAES efficiency impossible!
RIGHT thing to do is instead add a 2nd relationship: $\mathrm{P} V \mathrm{~m}=$ constant
This squirrely relationship describes a "Polytropic Process"
In it, the exponent $m$ depends on the "heat capacity" of the gas
$=\Delta$ Energy that must be added to raise gas temperature by one degree
If heating is "reversible" ( $\Delta$ Entropy $=0$ ), heat capacity is constant $=>m$ is constant
THEN polytropic equation can be substituted into ideal gas law to produce:
Description of how pressurization changes BOTH V and T
=> Efficiency limits of Compressed Air Storage (CAES) ${ }^{1-3}$

1) https://www.princeton.edu/pei/energy/publications/texts/SuccarWilliams_PEI_CAES_2008April8.pdf
2) http://content.lib.utah.edu/utils/getfile/collection/etd2/id/86/filename/1430.pdf
3) https://www.eeh.ee.ethz.ch/uploads/tx_ethpublications/Samaniego_2010.pdf

Challenge of heat loss => Multiple CAES versions:

The main ones are: DIABATIC CAES and ADIABATIC CAES

## But what the heck do diabatic and adiabatic mean?

A quick Google search on "adiabatic" (= non-diabatic):

## ad• $\cdot \mathrm{F} \cdot \mathrm{a} \cdot \mathrm{bat} \cdot \mathrm{ic}$

/,ādīə'batik, adēə-/ 4)
PHYSICS
adjective

1. relating to or denoting a process or condition in which heat does not enter or leave the system concerned.

## But Heat = Energy

So heat leaving a Compressed Air Energy Storage System = Energy lost Nevertheless, only diabatic (heat-loosing) CAES has been tried to date!

Contrasting the two main CAES approaches:

DIABATIC CAES (simple CAES) releases heat of compression to atmosphere
Which means that heat for re-expansion must come from other sources
If you've got plenty of time to wait, atmosphere can resupply the heat But you DON'T have time to wait with grid energy storage thus:

Heat for re-expansion is instead supplied by burning natural gas
=> LOW NET EFFICIENCY (total energy out / total energy put in)
THIS is scheme shown in preceding (and almost all other) CAES figures
ADIABATIC CAES traps both air and heat (as it is released)
This requires tanks/cavities that are BOTH pressure-tight AND heat-tight
So that stored heat can later be applied to re-heating \& expanding air
=> MUCH higher energy storage efficiencies, theoretically, up to $\sim 100 \%$

Compressed air energy storage numbers?
There are only two existing CAES plants worldwide, both diabatic (= heat wasting) Huntorf Germany (42\% efficient), McIntosh Alabama (54\% efficient)

But a large new adiabatic (heat trapping) plant is being built: German "ADELE"


Liberated heat is stored in above-ground tanks
By warming the liquids they contain
While compressed gas goes to buried caverns
These are recombined to expand gas
Design goals (upon planned completion in 2018):

- Round trip energy efficiency: 70\%
- Energy Storage: 1000 MW-h
- Footprint: ~ 1 hectare $=0.01$ km²

Did the ADELE CAES project achieve its 70\% efficiency goal?

In December of 2019, I searched the web for an answer
To my surprise, post 2017 information about ADELE was virtually non-existent
A few CAES review articles suggested that ADELE had achieved its $70 \%$ efficiency
Their apparent source was a single 2017 conference paper about ADELE
which stated in its abstract: 1
"After its completion in summer 2017 main achievements include the confirmation of a round-trip efficiency of about 70\%"

But within that paper, the relevant section discussed only modeled results, about alternate technologies, none even identified as being relevant to ADELE:
"Thermodynamic calculations for different plant calculations and TES technology options confirm a substantial cost reduction potential and improved operation flexibility, albeit with an acceptable decrease in efficiency compared to the adiabatic process. Depending on the specific system configuration and the level of permissible costs the round-trip efficiency ranges from 60 to $70 \%$ and somewhat above, with CAPEX below 280 €/kWh"

1) "Electricity storage with adiabatic compressed air energy storage: Results of the BMWi-project ADELE-ING" https://ieeexplore.ieee.org/document/8278771

## Another 2017 paper stated ADELE was on hold (possibly not even complete)

As published in the journal Energies (and posted by the University of Warwick) ${ }^{1}$
That article's (complete) discussion of ADELE reads:
"In Germany, as shown in Figure 15, the world's first large-scale AA-CAES project ADELE - with 70\% cycle efficiency cycle efficiency has been designed by RWE Power, General Electric and other partners. The aim of this project is to optimize the coexistence and smooth interaction of the individual energy sources, especially for wind power. It is planned to have 1 GWh storage capacity and be capable of generating up to 200 MW, said the RWE power. The ADELE project could provide backup capacity within a very short time and replace forty state-of-the-art wind turbines for a period of 5 h . The project is now on hold due to uncertain business conditions [61]."

Note that paragraph's recurrent use of future tense AND its final sentence
If that did not confuse matters enough, when I clicked on the link provided in reference [61], I was taken to a U.S. EIA webpage which not only contained zero information about CAES, much less about ADELE. Further, that webpage was dated "June 29, 2012" (i.e., years before ADELE's construction even began).

## Actual status of ADELE (or Adiabatic CAES in general)? Heck if I can figure it out!

1) "Overview of Compressed Air Energy Storage and Technology Development"
http://wrap.warwick.ac.uk/91858/7MRAP-overview-compressed-air-energy-storage-technology-development-Wang-2017.pdf
2) https://www. eia. gov/todayinenergy/detail.php?id=6910

## e) Energy storage via Capacitors or Super-Capacitors

As mentioned in an earlier lecture, capacitors sidestep Maxwell's 1st equation:
Trying to push more charge into an object doesn't really work:


Unless you fold the two plates over on top of one another:


No longer need charge balance on each plate
Excess +'s on top plate don't like one another
But repulsion's balanced by attraction to -'s below
Amount of charge stored is proportional to the pushing voltage: $\mathbf{Q}=\mathbf{C} \mathbf{V}(\mathbf{1})$
Constant $(C)=$ "Capacitance" of the capacitor - It increases the closer the plates are:
Capacitance $=$ Area $x$ (dielectric constant of material in gap) / (gap thickness)

$$
\begin{equation*}
\mathbf{C}=\varepsilon \text { Area / d } \tag{2}
\end{equation*}
$$

## But how much energy can a capacitor store?

Power of any type $=$ Energy flow $=>\quad P=\Delta E / \Delta t$
But electrical power $=$ voltage $\times$ current $=$ voltage $\times$ (charge flow)
Charge flow into a capacitor $=\Delta \mathrm{Q} / \Delta \mathrm{t}$ (change in charge stored per time)
So power into a capacitor is: $\quad P_{\text {capacitor }}=\mathrm{V} \times(\Delta \mathrm{Q} / \Delta \mathrm{T})$
Equations (3) and (4) BOTH give the power and are thus equal:
$\Delta \mathrm{E} / \Delta \mathrm{t}=\mathrm{V} \times(\Delta \mathrm{Q} / \Delta \mathrm{T})$ Or in calculus terms: $\quad \mathrm{dE} / \mathrm{dt}=\mathrm{V} d \mathrm{Q} / \mathrm{dT}$
But from equation (1), $\mathrm{Q}=\mathrm{CV}$, substituting this in: $\quad \mathrm{dE} / \mathrm{dt}=\mathrm{C} \mathrm{V} \mathrm{dV} / \mathrm{dT}$
Integrating over the capacitor's charging time: Energy capacitor $=1 / 2$ C V ${ }^{2}$
Doubled voltage applied to a capacitor => Quadrupled energy stored

## Design of a SUPER CAPACITOR:

Here we want huge energy storage per volume = energy storage density

$$
\text { Volume }_{\text {capactior }}=\text { Area }_{\text {capacitor }} \times \text { Thickness }_{\text {capacitor }}
$$

Simple capacitor:


Gray = metal plates $\quad$ White $=$ insulator

Thickness $_{\text {capacitor }}=2 \mathrm{~T}_{\text {plate }}+\mathrm{T}_{\text {insulator }}$

Then Energy stored in this stacked capacitor per volume is
Capacitor energy density $=$ C V $2 /\left[2 \times A \times\left(2 \mathrm{~T}_{\text {plate }}+\mathrm{T}_{\text {insulator }}\right)\right]$

So thinning down both the plates and insulators is a good idea, however:
Plates have to be thick enough that electron flow won't overheat them
Insulator has to be thick enough that electrons cannot jump through it

## This all suggests use of ultrathin nano materials

Which might allow for capacitors using single atom thick plates and insulators


But while there are extraordinarily good nano metals for the plates

## Nano insulators are NOT exceptionally good at blocking electron flow

Key phenomenon is called dielectric breakdown
Which occurs when the electric field across insulator exceeds $\boldsymbol{\xi}$ breakdown
Electrons then arc through, irreversibly damaging the insulator!
But electric field in insulator $=$ Capacitor voltage $/$ Thickness $_{\text {insulator }}=\mathrm{V} / \mathrm{T}_{\text {insulator }}$
To avoid breakdown, $T_{\text {insulator }}$ must thus increase in proportion to voltage used
But from earlier formula, energy stored in a capacitor increases as voltage squared
So despite need for thicker insulators
It still makes sense to use higher voltages in these capacitors As a conveniently "high" voltage, let's choose 110 volts (DC)

## Calculating required insulator thickness:



Choosing a nano insulator from the above figure: hexagonal boron nitride:
For $\mathbf{h - B N}, \boldsymbol{\xi}$ breakdown is $\mathbf{7 0 0 - 9 0 0} \mathbf{M V} /$ meter $^{1,2}$
For our voltage choice of 110 volts (DC) if we use h-BN for insulator then:
For no sparks, need $\mathrm{T}_{\mathrm{h} \text {-BN }}>110$ Volts / $(700 \mathrm{MV} / \mathrm{m}) \sim 160$ nanometers
For a safety margin, choose $T_{\text {h-BN insulator }}=200$ nanometers

Then calculating this "nano" capacitor's energy density:
Capacitor energy density $=$ C V ${ }^{2} /\left[2 \times\right.$ Area $\left.\times\left(T_{\text {plate }}+\mathrm{T}_{\text {insulator }}\right)\right]$
Where: $\mathrm{C}=\varepsilon$ Area $/ \mathrm{T}_{\text {insulator }}$

And for our choice of h-BN insulator using 110 VDC:

$$
\begin{aligned}
& T_{h-B N \text { insulator }}=200 \text { micron }=10^{-6} \mathrm{~m} \\
& T_{\text {insulator }} \gg T_{\text {plate }} \\
& \varepsilon_{\mathrm{h}-\mathrm{BN}}=\left(3 \text { to 4) } \times \varepsilon_{0}(1) \sim 30 \times 10^{-12} \mathrm{~s}^{4} \mathrm{Amp}^{2} / \mathrm{kg} \mathrm{~m}^{3}\right.
\end{aligned}
$$



Capacitor ${ }_{\text {energy density }} \sim\left(\varepsilon A / T_{\text {insulator }}\right) \mathrm{V}^{2} /\left(2 \mathrm{~A} \mathrm{~T}_{\text {insulator }}\right)=\varepsilon \mathbf{V}^{2} / 2 \mathrm{~T}_{\text {insulator }}{ }^{2}$
$=\left(3 \times 10^{-11} \mathrm{~s}^{4} \mathrm{Amp}^{2} / \mathrm{kg} \mathrm{m}^{3}\right)(110 \text { volts })^{2} / 2\left(0.2 \times 10^{-6} \mathrm{~m}\right)^{2}$

$$
=\left(3 \times 10^{-11}\right)\left(1.2 \times 10^{4}\right)(0.5)\left(2.5 \times 10^{13}\right)\left(\mathrm{s}^{2} \mathrm{~J} 2 / \mathrm{kg}-\mathrm{m}^{5}\right)=4.5 \mathrm{MJ} / \mathrm{m}^{3}=1.25 \mathrm{~kW}-\mathrm{h} / \mathrm{m}^{3}
$$

Likely efficiencies: ~ 100\%

## f) Energy storage via Super-Batteries

From note set on Batteries and Fuel Cells (pptx / pdf / key),
the top candidate might be flow batteries:
Which, recall, have this strange and complex configuration:


With two different electrolytes circulated in (via pumps) from external tanks
To a central cell with an "ion selective membrane"
Plus simple metal electrodes to either side

Molten sodium beta alumina batteries were a second candidate

## With overall structure:

- Central (anode) reservoir of molten sodium (green)
- Membrane capable of passing $\mathrm{Na}+$ ions (gray)

Typically: $\mathrm{Al}_{2} \mathrm{O}_{3}$ "beta alumina" ceramic

- Surrounding (cathode) outer cylinder (orange)

Typically: Sulfur / Sodium Sulfide $\left(\mathrm{Na}_{2} \mathrm{~S}_{x}\right)$


In the central anode:
$2 \mathrm{Na}=>2 \mathrm{Na}^{+}+2 \mathrm{e}^{-}$

At the outer cathode:

$$
\mathrm{xS}+2 \mathrm{Na}++2 \mathrm{e}^{-}=>\mathrm{Na}_{2} \mathrm{~S}_{\mathrm{x}}
$$

With $\mathrm{Na}+$ ions formed in anode migrating through beta alumina toward cathode

## Lithium ion batteries were a third candidate:

During CHARGING, Li is actually transferred from inside cathode to inside anode


DISCHARGE reverses this: Li transferred from inside the anode to inside cathode:

Anode:
Li desorbing and ionizing


Cathode:
Li absorbing and deionizing

## Comparative battery energy density data on all of these:




Ion flow energy density $=U \mathrm{Up}$ to $30 \mathrm{~kW}-\mathrm{h} / \mathrm{m}^{3}$
at ~ 73\% efficiency
Molten $\mathrm{Na}_{\text {energy density }}=$ Up to $270 \mathrm{~kW}-\mathrm{h} / \mathrm{m}^{3} \quad$ at $\sim 77 \%$ efficiency
Li Ion battery density $=\mathbf{U p}$ to $350 \mathrm{~kW}-\mathrm{h} / \mathrm{m}^{3}$

## g) Heat energy storage via Molten Salts

Best batteries returned $\sim 80 \%$ of electrical energy
Using electrical power in => electrical storage => electrical power out
Molten salts return only about 70\% of heat energy
A 10\% drop (compared to batteries) sounds significant
But while batteries are expensive, salt is cheap!
We might even mine AND store heat in the original SALT MINES!

NREL - Halotechnics Molten Salt Energy Storage Test Project, Emeryville CA:
$35.45 \mathrm{~kW}-\mathrm{h}$ stored in $0.19 \mathrm{~m}^{3}$ of salt, returning $25.1 \mathrm{kw}-\mathrm{h}(71 \%)^{1}$

Which gives:
Salt $_{\text {energy storage density }}=25.1 \mathrm{~kW}-\mathrm{h} / 0.19 \mathrm{~m}^{3}=132 \mathrm{~kW}-\mathrm{h} / \mathrm{m}^{3}$

FINALLY (!): Using ALL of the data from above:

To compute the impact of the most promising storage technologies when used in:
Scenario \#2 = Conventional Power + 8\% Storage:


Pumped Storage Hydro based energy storage SYSTEMS: 80\% efficiency
Bath PSH = 35.8 MW-h occupying ~ 2 km²
Number of plants: 887 GW-h / 35.8 MW-h = 24,781 plants
Cumulative national footprint: $(\sim 25,000) \times\left(\sim 2 \mathrm{~km}^{2}\right)=>\sim 50,000 \mathrm{~km}^{2}$

Fuel Cell based energy storage SYSTEMS: 30-35\% efficiency
"Planned" (future) plant capacity $=300$ MW-h:
Number of plants: 887 GW-h / 300 MW => 2,956 plants
Current test plant $=50 \mathrm{MW}-\mathrm{h}$, no info given on plant sizes
Number of plants: 887 GW-h / 50 MW => 17,740 plants
Cumulative national footprint: Not enough information given $=$ ? $\mathrm{km}^{2}$

Projected numbers for nation-wide energy storage SYSTEMS (cont'd):

Flywheel based energy storage SYSTEMS: 85-90\% efficeint
Current projects $=2$ MW-h occupying $\sim$ about 2 hectares
Number of plants: 887 GW-h / $(2$ MW-h $)=>443,500$ plants
Cumulative national footprint: ~ 90,000 hectares => $9000 \mathrm{~km}^{2}$

Adiabatic compressed air based energy storage SYSTEMS: 70\% efficient
Adiabatic plant (under construction) $=1000$ MW occupying $\sim 1$ hectare
Number of plants: : 887 GW-h / ( 1 GW-h) => 886 plants
Cumulative national footprint: $\sim 900$ hectares $=>9 \mathrm{~km}^{2}$

Projected numbers for nation-wide energy storage THINGS:

Based on assumptions: Volume $=887$ GW-h $/$ (energy storage density)
Converted to a footprint by assuming these are piled $\sim 1 \mathrm{~m}$ high in warehouses

Battery based energy storage THINGS: 70-80\% efficient
Energy Storage Density - Flow Batteries: $30 \mathrm{~kW}-\mathrm{h} / \mathrm{m}^{3}$
Cumulative volume $=>$ footprint: $29 \times 10^{6} \mathrm{~m}^{3}=>29 \mathrm{~km}^{2}$

Energy Storage Density - Molten Sodium Batteries: 270 kW-h/m³
Cumulative volume $=>$ footprint: $3.3 \times 10^{6} \mathrm{~m}^{3}=>3.3 \mathrm{~km}^{2}$

Energy Storage Density - Lithium Ion Batteries: $350 \mathrm{~kW}-\mathrm{h} / \mathrm{m}^{3}$
Cumulative footprint: $2.5 \times 10^{6} \mathrm{~m}^{3}=\mathbf{2 . 5} \mathrm{km}^{2}$

Projected numbers for nation-wide energy storage THINGS (cont'd):

Capacitor based energy storage THINGS: Iikely nearly 100\% efficient
Energy Storage Density - h-BN insulator : $1.25 \mathrm{~kW}-\mathrm{h} / \mathrm{m}^{3}$
Cumulative volume => footprint: $1.26 \times 10^{8} \mathrm{~m}^{3}=>126 \mathrm{~km}^{2}$

Molten Salt based ieat energy storage THINGS: 70\% efficient
Energy Storage Density: $132 \mathrm{~kW}-\mathrm{h} / \mathrm{m}^{3}$
Cumulative volume => footprint: $6.7 \times 10^{6} \mathrm{~m}^{3}=>6.7 \mathrm{~km}^{2}$

However, if you could get them to efficiently store
Salt Caverns might be a much better idea for cheap/large-scale storage

Leading to the somewhat surprising result:

In contrast to note set Power Plants Requirements: Land \& Water (pptx / pdf / key)

For this Scenario \#2 = Conventional Power + 8\% Storage

Land requirements of essentially all storage technologies are NOT excessive!

Indeed, especially for the technologies located primarily underground:
Surface ground use and overall environmental impact might be small

So WHY don't we already make extensive use of energy storage?

The answers must lie in:

## The Cost of Grid Scale Energy Storage

## NREL estimates of energy storage LCOEs:

## From a 2010 NREL presentation (with dashed lines giving anticipated 2015 costs):

Figure uses units of $\phi / k W-h r$ rather than more common units of $\$ / M W-h$ : $1 \Phi / k W-h r=>\$ 10 / M W-h$ (i.e. multiply by ten and change units)


An independent corporate study:
"Projections of the Levelized Cost Benefit of Grid Scale Energy Storage Options"
From a 2010 conference paper presented by Doty Energy Corp.
Final column gives levelized cost due to storage using the indicated technology

| Device | Storage Capacity | Peak Power | Storage Cost | Power Cost | Cycle Effic. | Mean Cycle Depth | Cycle Rate | Power Duty Cycle | Life Time | Incremental Cost of Energy |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| units | MWh | MW | \$/kWh | \$/kW | \% |  | cycle/yr |  | years | \$/MWh |
| Windfuels | 2000 | 100 | 0.05 | 900 | 0.52 | 0.5 | 320 | 0.5 | 30 | 38 |
| H2 fuel cell | 2800 | 120 | 10 | 540 | 0.7 | 0.4 | 320 | 0.4 | 10 | 51 |
| pumped hydro storage | 600 | 50 | 120 | 300 | 0.8 | 0.7 | 330 | 0.4 | 50 | 56 |
| UPHS | 550 | 40 | 120 | 500 | 0.75 | 0.7 | 320 | 0.4 | 50 | 68 |
| carbon-lead-acid battery | 750 | 70 | 100 | 250 | 0.75 | 0.4 | 500 | 0.3 | 10 | 102 |
| AA-CAES | 350 | 30 | 150 | 1200 | 0.61 | 0.55 | 320 | 0.3 | 30 | 162 |
| lithium-ion battery | 160 | 40 | 500 | 250 | 0.8 | 0.6 | 600 | 0.2 | 20 | 167 |
| lead-acid battery | 1100 | 100 | 60 | 250 | 0.75 | 0.5 | 250 | 0.2 | 5 | 181 |
| flywheel | 30 | 20 | 2800 | 500 | 0.85 | 0.7 | 800 | 0.1 | 30 | 532 |
| NaS battery | 75 | 9 | 1200 | 300 | 0.74 | 0.7 | 280 | 0.25 | 15 | 774 |
| ultra-capacitors | 5 | 5 | 20K | 400 | 0.7 | 0.7 | 1000 | 0.1 | 30 | 2910 |
| SMES | 0.6 | 0.2 | 150K | 700 | 0.5 | 0.6 | 300 | 0.1 | 30 | 94,000 |

A comparison of those data (all in \$/MW-h):

| Storage Technology | NREL LCOE <br> $\mathbf{2 0 1 0}$ | Doty LCOE <br> 2010 | NREL LCOE <br> $\sim$ |
| :--- | :--- | :--- | :--- |
| Pumped Storage Hydro | $130-180$ | 56 | 130 |
| Fuel Cell | $100-600$ | 51 | $240-280$ |
| V redox battery | $220-500$ |  | 280 |
| Adiabatic CAES | $100-165$ | 162 | 100 |
| Li ion battery |  | 167 |  |
| Flywheel |  | 532 |  |
| Lead Acid battery |  | 181 | 250 |
| NaS battery | $220-320$ | 774 | 830 |
| NiCd battery | $480-1030$ |  |  |
| Ultra Capacitors |  | 2910 |  |

## Quick analysis of storage LCOE's:

Pumped storage hydro (PSH / UPSH) is cheapest: ~ \$50 / MW-h
Fuel cell storage: Doty: Comparable to PSH NREL: 4-5 X PSH
Adiabatic CAES \& best battery storage ~ 2-3 X PSH = \$100-150 / MW-h
Storage LCOE would be ADDED to energy's production LCOE $=\$ 70-150 / \mathrm{MW}-\mathrm{h}$
Seemingly at least doubling or tripling the total cost of energy!
But not really, because under Scenario \#2:
Storage cost is added to only to the $\sim 8 \%$ of power we need to store
And competition = Scenario \#1 evening power, already 2-4X more expensive!


Thus some experts say storage could be competitive within five years

NEW Scenario 3: Use of ONLY "green" sustainable power sources
"Greenest" of renewable energy sources don't produce energy all of the time:
Examples include solar power, wind power, tidal power
And when they DO produce, it's not when we most need their production!
This, again, is how we LIKE to consume energy:

www.eia.gov/todayinenergy/detail.cfm?id=12711 YELLOW midnight lines added

These are data on actual wind speeds vs. time of day


TEXAS: www.seco.cpa.state.tx.us/publications/ renewenergy/windenergy.php



ONTARIO CANADA: www.omafra.gov.on.ca/english/ engineer/facts/03-047.htm


WISCONSIN: www. windpowerweather.com/history? date=last2days

Which, recalling that wind energy goes as wind velocity cubed:

Would lead to a typical wind energy versus time of day plot something like this:
( $\sim$ doubled afternoon wind speed $=>\sim 2^{3} \mathrm{X}$ wind power)
Thus, with wind energy peaking sharply in the late afternoon, we'd get power like:


## Solar energy peaks midday, but also varies by season:

Starts at sunrise, peaks at about noon, ends at sunset
And lasts longer and is more intense in the summer:


## Wholesale use of renewables => HUGE NEED for storage!

What we now need/want in the way of daily power:


What we'd get from a wind plant:

Noon
Midnight

What we'd get from a solar plant:


Let me (somewhat crudely) approximate either as half sine wave:


Area under half sinusoid $=$ Amplitude $x$ day $/ \mathrm{Pi}=\mathrm{P}_{\text {peak_renewable }} \mathrm{x}$ day $/ \mathrm{Pi}$
But if this to be all our power, this must $=80 \% \mathrm{P}_{\text {peak_use }} \mathrm{X}$ day

$$
\text { Implying } P_{\text {peak__renewable }}=0.8 \text { Pi } P_{\text {peak__use }}=2.5 \mathrm{P}_{\text {peak_use }}
$$

Whoops, so wind energy production would have to be more like:


## But I now need to store and shift ALL energy above green "use" line!

Yellow Base $\sim\left(0.8 P_{\text {peak_use }}\right)(\mathrm{d} / 2)=(0.4 \mathrm{~d})\left(\mathrm{P}_{\text {peak_renewable }} / 2.5\right)=0.16 \mathrm{P}_{\text {peak_renewable }} \mathrm{d}$
Fraction that must be stored and shifted = 1 - Yellow base / All

$$
=1-\left(0.16 P_{\text {peak_renewable }} d\right) /\left(P_{\text {peak_renewable }} d \text { day } / P i\right)=1-0.16 \mathrm{Pi}=50 \%
$$

Making this the "Green (only) Sustainables + 50\% Storage" scenario

## Whoops squared!

From previously having to store $\mathbf{8 \%}$ of energy to accommodate our power use curve

If we use single "green" renewable (i.e. neither hydro or nuclear), we would have to:
Store and shift 50\% of energy to accommodate our power use curve
Switch to renewables $=>$ Need to increase storage by $\sim 6 X$
(vs. storage Scenario \#2 which just eliminated evening "peaking" power plants)

Two renewables, peaking at different times (e.g. solar and wind) help a little Two renewables, coming from different time zones, help a little more

But this strongly suggests that we will have to retain some $24 / 7$ power sources
Producing a good fraction of the present day (Scenario \#1) base load
It's going to be really hard to abandon hydro \& nuclear power!

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